

1. A small marble is sliding horizontally along the ground with a speed of 4.0 m/s. It approaches a ramp, slides up it, and eventually comes to a stop before sliding back down the ramp. The friction between the marble and the ground is too small to make a difference to this problem.



- a. It helps to have a “feel” for how fast this marble is going. Convert the speed to miles per hour (MPH). [Curricular items 1a & 1b / 2 points]

$$(4.0\text{m} / 1\text{s})(1\text{km} / 1000\text{m})(1\text{mi} / 1.61\text{km})(3600\text{s} / 1\text{hr}) =$$

$$\boxed{8.94 \text{ mi/hr}}$$

- b. The marble is made from glass with a density of 2500 kg/m^3 . As you know, objects with density greater than water density (1 g/cm^3) will sink in water. Would this marble sink in water? Answer by converting the marble’s density to units appropriate for comparison with water. [Curricular items 1a & 1c / 2 points]

$$(2500\text{kg} / 1\text{m}^3)(1000\text{g} / 1\text{kg})(1^3\text{m}^3 / 100^3\text{cm}^3) =$$

$$\boxed{2.5 \text{ g/cm}^3 \text{ Yes, it would sink.}}$$

- c. What final height does the marble reach? (Show your work – remember that the highest grades are given to students who write a solution that can be understood by *everyone* in the class.) [Curricular item 5d / 6 points]

$$E_{\text{bottom}} = E_{\text{top}}$$

$$U_{\text{bottom}} + K_{\text{bottom}} = U_{\text{top}} + K_{\text{top}}$$

$$m g h_{\text{bottom}} + \frac{1}{2} m v_{\text{bottom}}^2 = m g h_{\text{top}} + \frac{1}{2} m v_{\text{top}}^2$$

$$g h_{\text{bottom}} + \frac{1}{2} v_{\text{bottom}}^2 = g h_{\text{top}} + \frac{1}{2} v_{\text{top}}^2$$

$$(10\text{m/s}^2)(0) + \frac{1}{2} (4\text{m/s})^2 = (10\text{m/s}^2) h_{\text{top}} + \frac{1}{2} (0)^2$$

$$8 \text{ m}^2/\text{s}^2 = (10 \text{ m/s}^2) h_{\text{top}}$$

$$\boxed{h_{\text{top}} = 0.8 \text{ m}}$$

2. The Earth is moving through space due to its orbit around the Sun with an average speed of 29.7 km/s. Calculate the kinetic energy of the Earth. (You may need to refer to your equation sheet for this problem.) [Curricular items 1a, 1b & 5b / 2 points]

$$v = (29.7 \text{ km} / 1 \text{ s})(1000 \text{ m} / 1 \text{ km}) = 29,700 \text{ m/s}$$

$$K = \frac{1}{2} m v^2$$

$$K = \frac{1}{2} (6 \times 10^{24} \text{ kg})(29700 \text{ m/s})^2$$

$$K = 2.646 \times 10^{33} \text{ J}$$

3. The radius of Mars is only half the radius of the Earth. So you might think there'd be less "real estate" available on Mars. However, 70% of the Earth's surface is covered with water. So: which planet has more *land area*? Justify your answer with a calculation or carefully written argument. (Note: surface area is calculated using the formula $SA = 4\pi R^2$ – this formula is available on your equation sheet.) [Curricular item 1c / 3 points]

Earth

$$SA = 4\pi(6.4 \times 10^6 \text{ m})^2$$

$$SA = 5.15 \times 10^{14} \text{ m}^2$$

$$\text{Land Area} = 0.3(SA) = 0.3(5.15 \times 10^{14} \text{ m}^2)$$

$$\text{Land Area} = 1.5 \times 10^{14} \text{ m}^2$$

Mars

$$SA = 4\pi(3.2 \times 10^6 \text{ m})^2$$

$$SA = 1.3 \times 10^{14} \text{ m}^2$$

$$\text{Land Area} = SA = 1.3 \times 10^{14} \text{ m}^2$$

Earth still has more land area. In fact it has about 15% more:

$$1.5 \times 10^{14} \text{ m}^2 / 1.3 \times 10^{14} \text{ m}^2 = 1.15$$

4. The Olympic gold medal in women's diving this year went to Chen Ruolin. The diving board was 10.0 m above the surface of the water. Assume Chen Ruolin began by launching off the board with a speed of 3.0 m/s. At what speed did she hit the water? *Please include an energy bar graph in your solution.* [Curricular items 5a & 5d / 5 points]



$$E_{\text{bottom}} = E_{\text{top}}$$

$$U_{\text{bottom}} + K_{\text{bottom}} = U_{\text{top}} + K_{\text{top}}$$

$$m g h_{\text{bottom}} + \frac{1}{2} m v_{\text{bottom}}^2 = m g h_{\text{top}} + \frac{1}{2} m v_{\text{top}}^2$$

$$g h_{\text{bottom}} + \frac{1}{2} v_{\text{bottom}}^2 = g h_{\text{top}} + \frac{1}{2} v_{\text{top}}^2$$

$$(10 \text{ m/s}^2)(0) + \frac{1}{2} v_{\text{bottom}}^2 = (10 \text{ m/s}^2)(10 \text{ m}) + \frac{1}{2}(3 \text{ m/s})^2$$

$$\frac{1}{2} v_{\text{top}}^2 = 100 \text{ m}^2/\text{s}^2 + 4.5 \text{ m}^2/\text{s}^2$$

$$\frac{1}{2} v_{\text{top}}^2 = 104.5 \text{ m}^2/\text{s}^2$$

$$v_{\text{top}}^2 = 209 \text{ m}^2/\text{s}^2$$

$$v_{\text{bottom}} = 14.46 \text{ m/s}$$

